Convention, Accuracy metrics, Classification, Regression

Nipun Batra

January 11, 2024

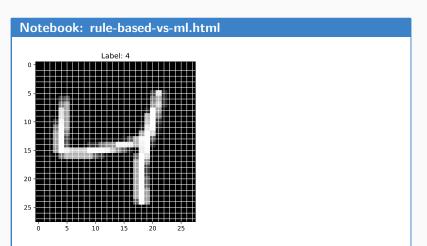
IIT Gandhinagar

- PoseNet Whole
- Blog post from Google
- Rock Papers Scissors

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Let us work on digit recognition problem.



• How would you program to recognise digits? Start with 4.

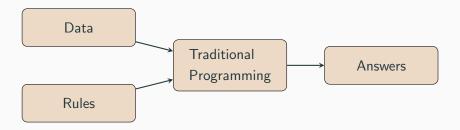
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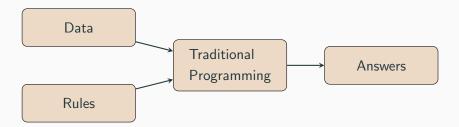
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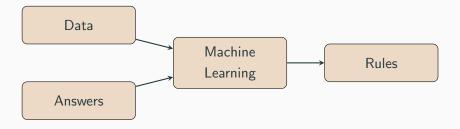
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- There can be some cases of 4 where the first | is at 45 degrees
- There can be some cases of 4 where the width of each stroke is different







"A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P if its performance at tasks in T, as measured by P, improves with experience E." - Tom Mitchell

Problem statement: You want to predict the quality/condition of a tomato given its visual features.



- Size
- Colour

- Size
- Colour
- Texture

Imagine you have some past data on quality of tomatoes.

Sample	Colour	Size	Texture	Condition
1	Orange	Small	Smooth	Good
2	Red	Small	Rough	Good
3	Orange	Medium	Smooth	Bad
4	Yellow	Large	Smooth	Bad

Is the sample number a useful feature for predicting quality of a tomato?

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Answer: It depends! Maybe, all tomatoes received after a certain date are bad! Let us ignore that for now.

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Let us modify our data table for now.

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Red	Small	Rough	Good
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The training set consists of two parts:

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1. Features, Attributes or Covariates

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The training set consists of two parts:

- 1. Features, Attributes or Covariates
- 2. Output or Response Variable

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Orange	Small	Smooth	Good
Red	Small	Rough	Good
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Colour	Size	Texture	Condition
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We call this matrix as \mathcal{D} , containing:

Colour	Size	Texture	Condition
Orange	Small	Smooth	Good
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Yellow	Large	Smooth	Bad

We call this matrix as \mathcal{D} , containing:

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• Thus,
$$\mathbf{X} = \{x_i^T\}_{i=1}^N$$
 where $x_i \in \mathcal{R}^P$

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We call this matrix as \mathcal{D} , containing:

• Thus,
$$\mathbf{X} = \{x_i^T\}_{i=1}^N$$
 where $x_i \in \mathcal{R}^F$
• Example $x_1 = \begin{bmatrix} Orange \\ Small \\ Smooth \end{bmatrix}$

Colour	Size	Texture	Condition
Orange	Small	Smooth	Good
Red	Small	Rough	Good
Orange	Medium	Smooth	Bad
Yellow	Large	Smooth	Bad

We call this matrix as \mathcal{D} , containing:

- 1. Feature matrix $(\mathbf{X} \in \mathcal{R}^{\mathbf{N} \times \mathbf{P}})$ containing data of N samples each of which is P dimensional.
 - Thus, $\mathbf{X} = \{x_i^T\}_{i=1}^N$ where $x_i \in \mathcal{R}^P$ • Example $x_1 = \begin{bmatrix} Orange \\ Small \\ Smooth \end{bmatrix}$
- Output Vector (y ∈ R^N) containing output variable for N samples.

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Orange	Small	Smooth	Good
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• Thus,
$$\mathbf{X} = \{x_i^T\}_{i=1}^N$$
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• Example $x_1 = \begin{bmatrix} Orange \\ Small \\ Smooth \end{bmatrix}$

- Output Vector (y ∈ R^N) containing output variable for N samples.
- 3. Thus, we can also write $\mathcal{D} = \{(x_i^T, y_i)\}_{i=1}^N$

Estimate condition for unseen tomatoes (#5, 6) based on data set.

Colour	Size	Texture	Condition
Orange	Small	Smooth	Good
Red	Small	Rough	Good
Orange	Medium	Smooth	Bad
Yellow	Large	Smooth	Bad
Red	Large	Rough	?
Orange	Large	Rough	?

Testing set is similar to training set, but, does not contain labels for output variable.

Colour	Size	Texture	Condition
Orange	Small	Smooth	Good
Red	Small	Rough	Good
Orange	Medium	Smooth	Bad
Yellow	Large	Smooth	Bad
Red	Large	Rough	?
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- 1. Learn f: Condition = f(colour, size, texture)
- 2. From Training Dataset
- 3. To Predict the condition for the Testing set

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Orange	Small	Smooth	Good
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- Q: Is predicting on test set enough to say our model generalises?
- A: Ideally, no!
- Ideally we want to predict "well" on all possible inputs. But, can we test that?
- No! Since, the test set is only a sample from all possible inputs.

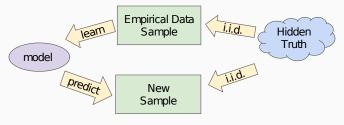


Image courtesy Google ML crash course

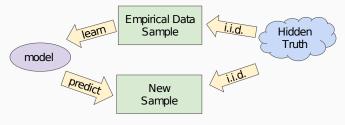


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Both the training set and the test set are samples drawn from the hidden true distribution (also sometimes called population)

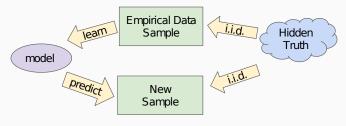


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More discussion later once we study bias and variance

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Question: What factors does the campus energy consumption depend on?

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# People	Temp (C)	Energy (kWh)
4000	30	30
4200	30	32
4200	35	40
3000	20	?
1000	45	?

• Classification

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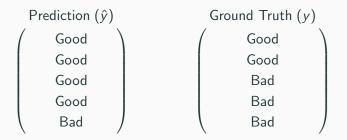
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 - Output variable is continuous
 - i.e. $y_i \in \mathcal{R}$

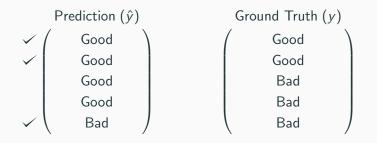
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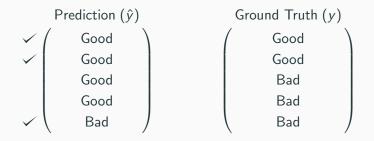
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 - Output variable is continuous
 - i.e. $y_i \in \mathcal{R}$
 - Examples Predicting:
 - How much energy will campus consume?
 - How much rainfall will fall?



Ground Truth: From the actual training set Prediction: Made by the model Accuracy

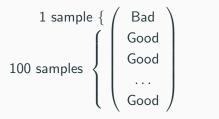


Accuracy



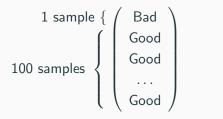
$$\begin{aligned} \mathsf{Accuracy} &= \frac{||y = \hat{y}||}{||y||} \\ &= \frac{3}{5} = 0.6 \end{aligned}$$

Types of Data: Imbalanced Classes



Imbalanced Classes

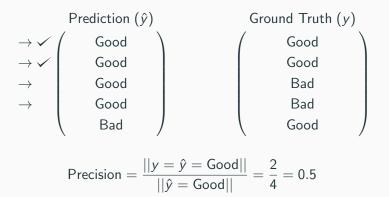
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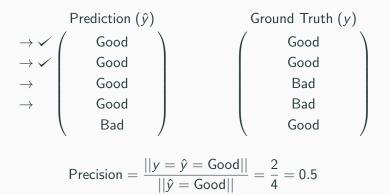
Imbalanced Classes

Cases for this:

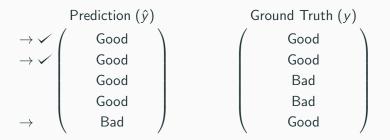
- Cancer Screening
- Planet Detection



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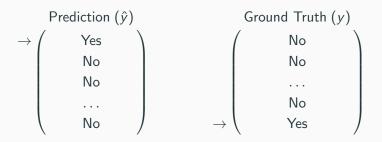


$$\text{Recall} = \frac{||y = \hat{y} = \text{Good}||}{||y = \text{Good}||} = \frac{2}{3} = 0.67$$

"the fraction of the total amount of relevant instances that were actually retrieved"

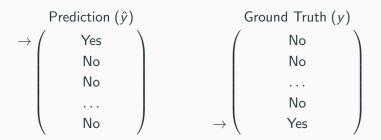
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Given predictions of whether a tissue is cancerous or not (n = 100).



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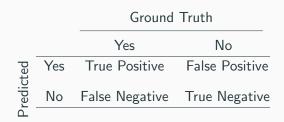
Accuracy
$$=$$
 $\frac{98}{100} = 0.98$ Recall $=$ $\frac{0}{1} = 0$
Precision $=$ $\frac{0}{1} = 0$

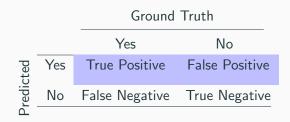
Accuracy Metrics: Confusion Matrix

		Ground Truth	
		Yes	No
ted	Yes	0	1
redicted	No	1	98
Р			

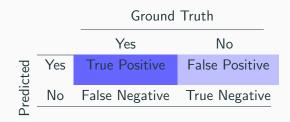
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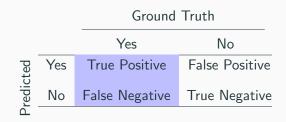




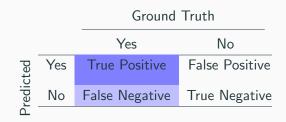
$$\mathsf{Precision} = \frac{T.P.}{T.P.+F.P.}$$



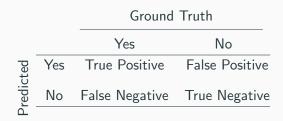
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$$F-Score = \frac{2 \times Precision \times Recall}{Precision + Recall}$$

		Ground Truth	
		Yes	No
cted	Yes	True Positive	False Positive
redicted	No	False Negative	True Negative

 $\begin{array}{l} \mbox{Matthew's correlation coefficient} = \\ \frac{\mbox{TP} \times \mbox{TN} - \mbox{FP} \times \mbox{FN}}{\sqrt{(\mbox{TP} + \mbox{FP})(\mbox{TP} + \mbox{FN})(\mbox{TN} + \mbox{FP})(\mbox{TN} + \mbox{FN})}} \end{array}$

For the data given below, calculate:

$$\begin{array}{c} \text{G.T. Positive} \quad \text{G.T. Negative} \\ \text{Pred Positive} \begin{pmatrix} 90 & 4 \\ 1 & 1 \end{pmatrix} \end{array}$$

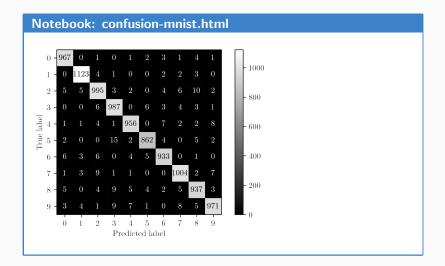
Precision = ? Recall = ? F-Score = ? Matthew's Coeff. = ?

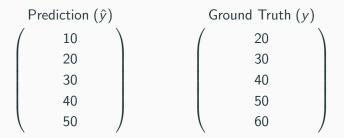
For the same data

G.T. Positive G.T. Negative
Pred Positive
$$\begin{pmatrix} 90 & 4 \\ 1 & 1 \end{pmatrix}$$

 $\begin{array}{l} \mbox{Precision} = \frac{90}{94} \\ \mbox{Recall} = \frac{90}{91} \\ \mbox{F-Score} = 0.9524 \\ \mbox{Matthew's Coeff.} = 0.14 \end{array}$

Confusion Matrix for multi-class classification





Mean Squared Error (MSE) = $\frac{\sum_{i=1}^{N} (\hat{y}_i - y_i)^2}{N}$ Root Mean Square Error (RMSE) = \sqrt{MSE}

Accuracy Metrics: MAE & ME

Prediction (\hat{y})	Ground Truth
$\begin{pmatrix} 10 \end{pmatrix}$	$\begin{pmatrix} 20 \end{pmatrix}$
20	30
30	40
40	50
50	60

Mean Absolute Error (ME) = $\frac{\sum_{i=1}^{N} |\hat{y}_i - y_i|}{N}$ Mean Error = $\frac{\sum_{i=1}^{N} \hat{y}_i - y_i}{N}$

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Is there any downside with using mean error?

Accuracy Metrics: MAE & ME

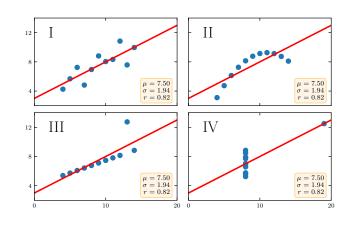
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Is there any downside with using mean error? Errors can get cancelled out

The Importance of Plotting





Anscombe's Quartet

Notebook: dummy-baselines.html

Property	Value	Accross datasets
mean(X)	9	exact
mean(Y)	7.5	upto 3 decimal places
Linear regression line	y = 3.00 + 0.500x	upto 2 decimal places