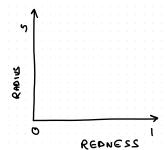
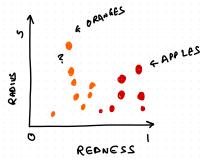
K-Nearest Neighbors

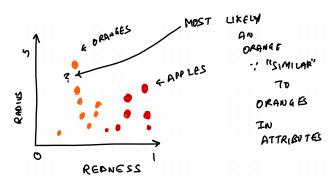
Nipun Batra July 5, 2020

IIT Gandhinagar

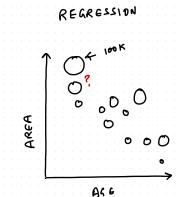


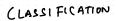








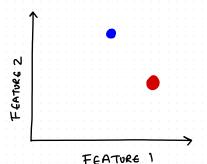




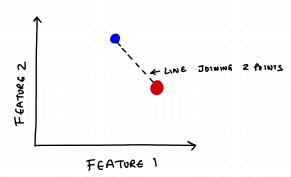
REGRESSION



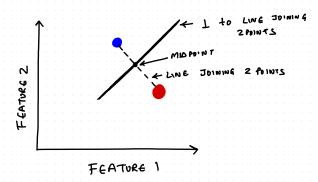
VORONOI DIAGRAM FOR I-NA

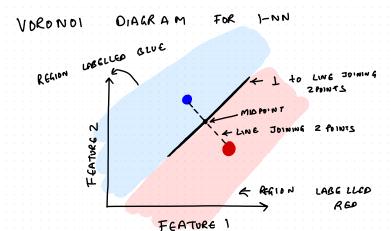


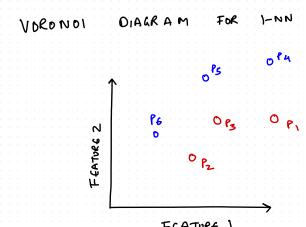
VARONOL DIAGRAM FOR I-NN



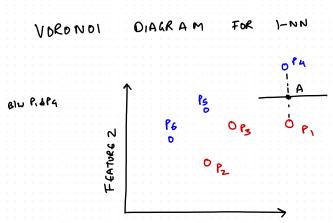
VINRONOL DIAGRAM FOR I-NN

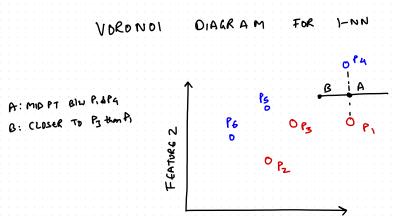


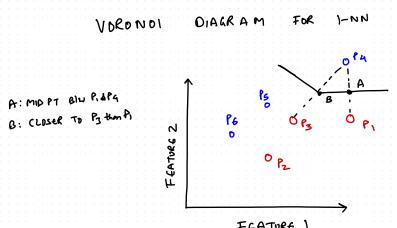


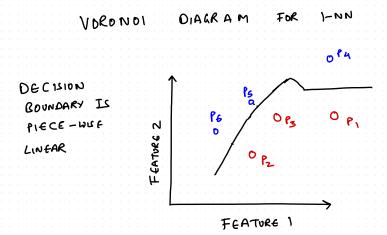


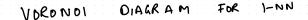
DIAGR A M FEATURE :

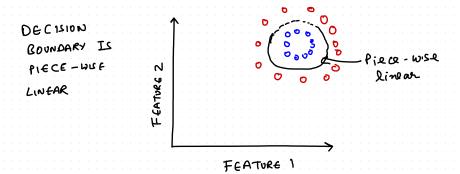






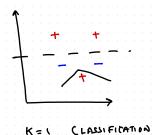




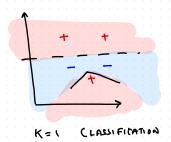


KNN CLASSI FICATION

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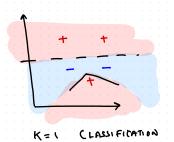


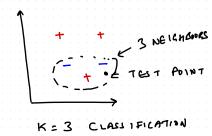
CNN CLASSI FICATION



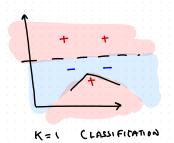


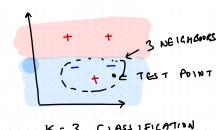
CNN CLASSI FICATION



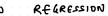


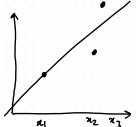
CNN CLASSI FICATION

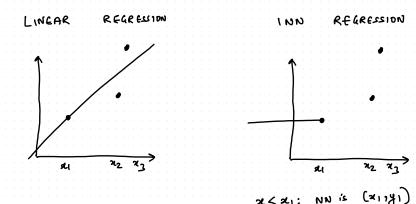


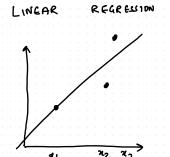


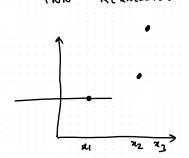
LINCAR REGRESSION

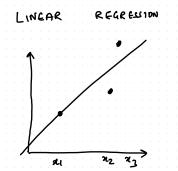


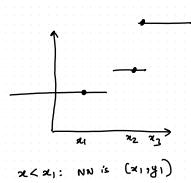












KNN IS NON- PARAMETRIC

MODEL

LINEAR

IS NOW- PARAMETRIC

LINEAR MODEL

y = matc (# params = 2)

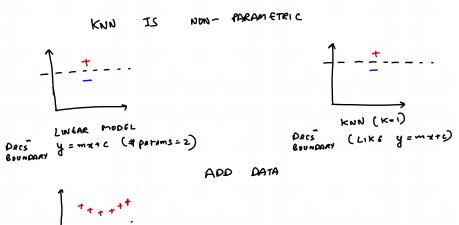
KNN IS NOW- PARAMETRIC

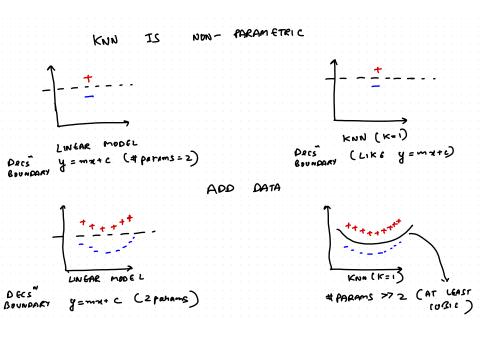
LINEAR MODEL

S Y = matc (# params = 2)

Dacs

Boundary (LIKE Y = mate





Parametric vs Non-Parametric Models

	Parametric	Non-Parametric
Parameter	Number of param-	Number of parame-
	eters is fixed w.r.t	ters grows w.r.t. to an
	dataset size	increase in dataset
		size
Speed	Quicker (as the	Longer (as number
	number of parame-	of parameters are
	ters are less)	less)
Assumptions	Strong Assumptions	Very few (sometimes
	(like linearity in Lin-	no) assumptions
	ear Regression)	
Examples	Linear Regression	KNN, Decision Tree

Lazy vs Eager Strategies

	Lazy	Eager
Train Time	0	≠ 0
Test	Long (due to com-	Quick (as only
	parison with train	"parameters" are
	data)	involved)
Memory	Store/Memorise en-	Store only learnt pa-
	tire data	rameters
Utility	Useful for online	
	settings	
Examples	KNN	Linear Regression,
		Decision Tree

Important Considerations

 What are the features that will be considered for data similarity?

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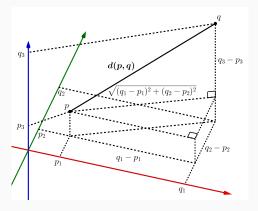
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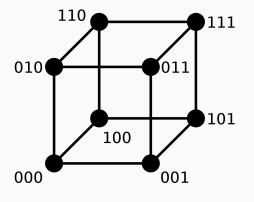
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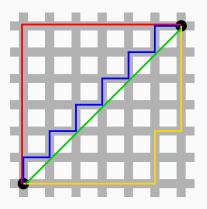
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- · What is the aggregation function that is going to be used?
- What are the number of neighbors that you are going to take into consideration?
- What is the computational complexity of the algorithm that you are implementing?



Euclidean Distance



Hamming Distance



Manhattan Distance

Choosing the correct value of K is difficult.

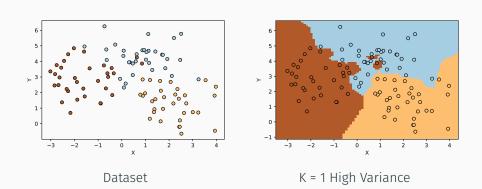
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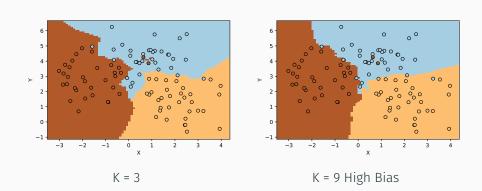
Low values of K will result in each point having a very high influence on the final output \implies noise will influence the result

Choosing the correct value of K is difficult.

Low values of K will result in each point having a very high influence on the final output \implies noise will influence the result

High values of K will result in smoother decision boundaries ⇒ lower variance but also higher bias





Aggregating data

There are different ways to go about aggregating the data from the K nearest neighbors.

- Median
- Mean
- · Mode

• Keep the entire dataset: (x, y)

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- For a query vector *q*:

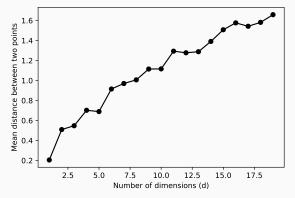
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 - 1. Find the k-closest data point(s) x^*

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- For a query vector q:
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 - 2. Predict *y**

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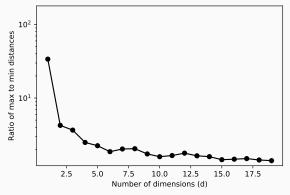
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For a unifromly random dataset

With an increase in the number of dimensions:

- 1. the distance between points starts to increase
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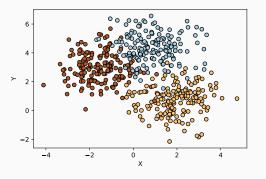
For a unifromly random dataset

With an increase in the number of dimensions:

- 1. the distance between points starts to increase
- 2. the variation in distances between points starts to decrease

Due to this, distance metrics lose their efficacy as a similarity metric.

Doing an exhaustive search over all the points is time consuming, especially if you have a large number of data points.



Example of a big dataset

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Such techniques include:

- Locality sensitive hashing
- Vector approximation files

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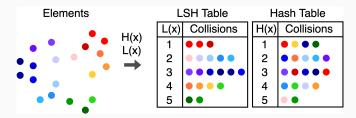
If you are willing to sacrifice accuracy there are algorithms that can give you improvements that go into orders of magnitude.

Such techniques include:

- · Locality sensitive hashing
- · Vector approximation files
- Greedy search in proximity neighborhood graphs

Locality sensitive hashing

Normal hash functions H(x) try to keep the collision of points across bins uniform.

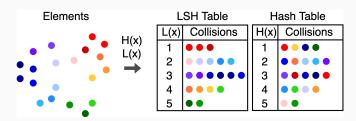


Example of a big dataset

Locality sensitive hashing

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A locality sensitive hash (LSH) function L(x) would be designed such that similar values are mapped to similar bins.

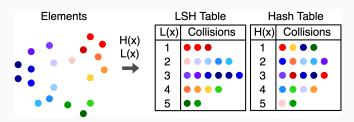


Example of a big dataset

Locality sensitive hashing

A locality sensitive hash (LSH) function L(x) would be designed such that similar values are mapped to similar bins.

For such cases, all elements in a bin would be given the same label, which again can be decided on the basis of different aggregation methods



Example of a big dataset