## Convolutional Neural Networks

## Imagenet

14 million images, 20K categories


## Imagenet

IT'S NOT ABOUT THE ALGORITHM
The data that transformed AI
research-and possibly the world
July 26, 2017
By Dave Gershgorn
Contributor


## Imagenet

- Circa 2006, Al community: "a better algorithm would make better decisions, regardless of the data."
- Fei Fei Li thought: "the best algorithm wouldn't work well if the data it learned from didn't reflect the real world"
- "We decided we wanted to do something that was completely historically unprecedented," Li said, referring to a small team who would initially work with her. "We're going to map out the entire world of objects.


## Imagenet

- ImageNet: published in 2009 as a research poster stuck in the corner of a Miami Beach conference center, the dataset quickly evolved into an annual competition to see which algorithms could identify objects in the dataset's images with the lowest error rate.
- "The paradigm shift of the ImageNet thinking is that while a lot of people are paying attention to models, let's pay attention to data," Li said. "Data will redefine how we think about models."


## WordNet





 trembo ste dida datiel afr migiar









vinbery rate mom a a asar'
 -5 antintin
 nodhung

## WordNet

- In the late 1980s, Princeton psychologist George Miller started a project called WordNet, with the aim of building a hierarchical structure for the English language.
- For example, within WordNet, the word "dog" would be nested under "canine," which would be nested under "mammal," and so on. It was a way to organize language that relied on machine-readable logic, and amassed more than 155,000 indexed words.


## Back to Imagenet

- Finding the perfect algorithm seemed distant, Li says. She saw that previous datasets didn't capture how variable the world could be—even just identifying pictures of cats is infinitely complex.
- If you only saw five pictures of cats, you'd only have five camera angles, lighting conditions, and maybe variety of cat. But if you've seen 500 pictures of cats, there are many more examples to draw commonalities from.
- Having read about WordNet's approach, Li met with professor Christiane Fellbaum, a researcher influential in the continued work on WordNet, during a 2006 visit to Princeton. Fellbaum had the idea that WordNet could have an image associated with each of the words, more as a reference rather than a computer vision dataset.


## Back to Imagenet

- Li's first idea was to hire undergraduate students for $\$ 10$ an hour to manually find images and add them to the dataset. But back-of-the-napkin math quickly made Li realize that at the undergrads' rate of collecting images it would take 90 years to complete.
- Undergrads were time-consuming, algorithms were flawed, and the team didn't have money—Li said the project failed to win any of the federal grants she applied for, receiving comments on proposals that it was shameful Princeton would research this topic, and that the only strength of proposal was that Li was a woman.
- A solution finally surfaced in a chance hallway conversation with a graduate student who asked Li whether she had heard of Amazon Mechanical Turk, a service where hordes of humans sitting at computers around the world would complete small online tasks for pennies.


## Back to Imagenet

Main Inutructions Unsawe? Look up in Wiopeda Googhn [Addidionat inpur] Ho good photos? Have expertise? comments? Click heret

## First time workers please click here for instructions.

Click an the photos that contain the object or depict the concept of delta a low triangular area of alluvial deposits where a river divides before antering a larger body of water; The Mississippl River delta"; "The Nile delta", (PIEASE READ DEFPMOOUCAREFULLY)


Below are the photos you have selected FROM THIS PAGE ONLY the image: to other pages ) Click to deselect.


## Back to Imagenet

- Even after finding Mechanical Turk, the dataset took two and a half years to complete. It consisted of 3.2 million labelled images, separated into 5,247 categories, sorted into 12 subtrees like "mammal," "vehicle," and "furniture."
- In 2009, Li and her team published the ImageNet paper with the dataset-to little fanfare. Li recalls that CVPR, a leading conference in computer vision research, only allowed a poster, instead of an oral presentation, and the team handed out ImageNet-branded pens to drum up interest. People were skeptical of the basic idea that more data would help them develop better algorithms.
- "There were comments like 'If you can't even do one object well, why would you do thousands, or tens of thousands of objects?"

ImageNet Large Scale Visual Recognition Challenge results


In 2012, the team to first use deep learning was the only team to get their error rate below $25 \%$.

The following year nearly every team got $25 \%$ or fewer wrong

## In 2017, 29 of 38

 teams got less than 5\% wrong.

14 million images, 20K categories
empetition's first yea
eams had varying success.
Every team got at least 25\%
wrong.
'16
'17

## History (AlexNet 2012)



## History (LeCun 1998)



## Modern day cameras

TOP BRANDS - 2017
The most popular brands used by the Flickr community
(Percentage of photographers)


## Modern day cameras

## n

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## Mi Note 10 is coming

World's first 108MP penta camera


## Modern day cameras suitability for MLPs?



Courtesy:
https://www.superdatascience.com/convolutional-neural-networ ks-cnn-step-4-full-connection/

## Modern day cameras suitability for MLPs?



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1. If we are classifying cats vs dogs and hidden layer size is 100, what is number of parameters?

## Modern day cameras suitability for MLPs?



## Courtesy:

https://www.superdatascience.com/convolutional-neural-networ ks-cnn-step-4-full-connection/

1. If we are classifying cats vs dogs and hidden layer size is 100 , what is number of parameters?
2. $\mathrm{N}[1]=100, \mathrm{~N}[0]=$ 108*1M*3 (for RGB channel) $\rightarrow$ Billions of params
3. Size of weight matrix assuming each param is 32 bytes is 32
bytes*324 billion $\rightarrow$ several GBs

## Are MLPs well suited for images?



Courtesy:
https://www.rd.com/advice/pets/commo
n-cat-myths/


Courtesy:
https://www.goodhousekeeping.com/lif e/pets/g21525625/why-cats-are-best-p ets/

Are both of the above cats?

## Are MLPs well suited for images?



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n-cat-myths/


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https://www.goodhousekeeping.com/lif e/pets/g21525625/why-cats-are-best-p ets/

Assume both are 100X100 images and bounded rectangle are 10X10 pixels

## Are MLPs well suited for images?



Courtesy:
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n-cat-myths/


Courtesy:
https://www.goodhousekeeping.com/lif e/pets/g21525625/why-cats-are-best-p ets/

A cat ear is a cat ear, irrespective of the location in the image.
MLP would see these are different input features
Rather, we need "feature detector" that is translation invariant.

## Are MLPs well suited for images?



Courtesy:
https://www.rd.com/advice/pets/commo
n-cat-myths/


Courtesy:
https://www.goodhousekeeping.com/lif e/pets/g21525625/why-cats-are-best-p ets/

MLPs assume all input features to be independent
But, we have a spatially local structure, nearby pixels are similar

## Key Idea



Courtesy:
https://www.rd.com/advice/pets/commo
n-cat-myths/

## Build local feature detectors



Courtesy:
https://www.goodhousekeeping.com/lif e/pets/g21525625/why-cats-are-best-p ets/

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)
Filter

| 0 | 1 | 2 |
| :--- | :--- | :--- |
| 2 | 2 | 0 |
| 0 | 1 | 2 |

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)

Input

| $3_{0}$ | $3_{1}$ | $2_{2}$ | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| $0_{2}$ | $0_{2}$ | $1_{0}$ | 3 | 1 |
| $3_{0}$ | $1_{1}$ | $2_{2}$ | 2 | 3 |
| 2 | 0 | 0 | 2 | 2 |
| 2 | 0 | 0 | 0 | 1 |

Output

| 12.0 | 12.0 | 17.0 |
| :---: | :---: | :---: |
| 10.0 | 17.0 | 19.0 |
| 9.0 | 6.0 | 14.0 |

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)

Input
Output

| 3 | $3_{0}$ | $2_{1}$ | $1_{2}$ | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | $0_{2}$ | $1_{2}$ | $3_{0}$ | 1 |
| 3 | $1_{0}$ | $2_{1}$ | $2_{2}$ | 3 |
| 2 | 0 | 0 | 2 | 2 |
| 2 | 0 | 0 | 0 | 1 |


| 12.0 | 12.0 | 17.0 |
| :---: | :---: | :---: |
| 10.0 | 17.0 | 19.0 |
| 9.0 | 6.0 | 14.0 |

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)

Notebook demonstration (edge detection)

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)

Given input image of n Xn and filter of size: f Xf , what is the size of the output?

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)

Given input image of n Xn and filter of size: f Xf , what is the size of the output?
$n-f+1 \times n-f+1$

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)

Start with a $32 \times 32$ image and repeated operations of a single 5 X 5 filter, after how many such operations will we have a $1 \times 1$ output?

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(A guide to convolution arithmetic for deep learning)

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| Iteration | n | f | $\mathrm{n}-\mathrm{f}+1$ |
| :--- | :--- | :--- | :--- |
| 1 | 32 | 5 | 28 |
| 2 | 28 | 5 | 24 |
| 3 | 24 | 5 | 20 |
| 4 | 20 | 5 | 16 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)


Start with a $32 \times 32$ image and repeated operations of a single $5 \times 5$ filter, after how many such operations will we have a $1 \times 1$ output?

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| :--- | :--- | :--- | :--- |
| 1 | 32 | 5 | 28 |
| 2 | 28 | 5 | 24 |
| 3 | 24 | 5 | 20 |
| 4 | 20 | 5 | 16 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)

| 3 | $3_{0}$ | $2_{1}$ | $1_{2}$ | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | $0_{2}$ | $1_{2}$ | $3_{0}$ | 1 |
| 3 | $1_{0}$ | $2_{1}$ | $2_{2}$ | 3 |
| 2 | 0 | 0 | 2 | 2 |
| 2 | 0 | 0 | 0 | 1 |

How many times is left-most pixel used in a calculation?

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)

| 3 | $3_{0}$ | $2_{1}$ | $1_{2}$ | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | $0_{2}$ | $1_{2}$ | $3_{0}$ | 1 |
| 3 | $1_{0}$ | $2_{1}$ | $2_{2}$ | 3 |
| 2 | 0 | 0 | 2 | 2 |
| 2 | 0 | 0 | 0 | 1 |

How many times is left-most pixel used in a calculation?

Only once!

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)

| 3 | $3_{0}$ | $2_{1}$ | $1_{2}$ | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | $0_{2}$ | $1_{2}$ | $3_{0}$ | 1 |
| 3 | $1_{0}$ | $2_{1}$ | $2_{2}$ | 3 |
| 2 | 0 | 0 | 2 | 2 |
| 2 | 0 | 0 | 0 | 1 |

How many times is left-most pixel used in a calculation?

Only once!

How many times is a middle pixel used in a calculation?

Many times. For example, the middle pixel with value 2 used nine times!

## Building Block: Filters and Convolution Operation

(A guide to convolution arithmetic for deep learning)

| 3 | $3_{0}$ | $2_{1}$ | $1_{2}$ | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | $0_{2}$ | $1_{2}$ | $3_{0}$ | 1 |
| 3 | $1_{0}$ | $2_{1}$ | $2_{2}$ | 3 |
| 2 | 0 | 0 | 2 | 2 |
| 2 | 0 | 0 | 0 | 1 |

How many times is left-most pixel used

Problem 2: The corner pixels are under-utilised
in a calculation?

Only once!

How many times is a middle pixel used in a calculation?


Many times. For example, the middle pixel with value 2 used nine times!

## Building Block: Padding

| Input |  |  |  |  |  |  |  | Padded pixels |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0{ }_{0}$ | $0_{1}$ | $\mathrm{O}_{2}$ | 0 | 0 | 0 | 0 |  |  |  |
| $0_{2}$ | 32 | 3 | 2 | 1 | 0 | 0 |  | Outpu |  |
| $0_{0}$ | $0_{1}$ | 0 | 1 | 3 | 1 | 0 | 6.0 | 17.0 | 3.0 |
| 10 | 3 | 1 | 2 | 2 | 3 | 0 | 8.0 | 17.0 | 13.0 |
| 10 | 2 | 0 | 0 | 2 | 2 | 0 | 6.0 | 4.0 | 4.0 |
| 10 | 2 | 0 | 0 | 0 | 1 | 0 i |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

## Building Block: Padding

|  | $\mathrm{O}_{2}$ | 5? |  |
| :---: | :---: | :---: | :---: |
|  |  | 2 |  |
| 0 |  | 1 |  |
|  |  |  |  |
|  |  | 02 |  |
|  |  |  |  |


\section*{| 6.0 | 17.0 | 3.0 |
| :---: | :---: | :---: |
| 8.0 | 17.0 | 13.0 |
| 6.0 | 4.0 | 4.0 |}



## Building Block: Padding



Ques: Given padding of $\mathbf{p}$ pixel, $\mathbf{n} \mathbf{X} \mathbf{n}$ image and filter $\mathbf{f} \mathbf{x} \mathbf{f}$, what is the output size?

## Building Block: Padding



Ques: Given padding of $\mathbf{p}$ pixel, $\mathbf{n} \mathbf{X} \mathbf{n}$ image and filter $\mathbf{f} \mathbf{x} \mathbf{f}$, what is the output size?
$n+2 p-f+1 \times n+2 p-f+1$

## Building Block: Padding



Ques: Given padding of $\mathbf{p}$ pixel, $\mathbf{n} \mathbf{X} \mathbf{n}$ image and filter $\mathbf{f} \mathbf{x} \mathbf{f}$, what is the output size?
$n+2 p-f+1 \times n+2 p-f+1$

Same padding: when $n+2 p-f+1=n$ or, $p=(f-1) / 2$

## Building Block: Strides (subsampling)

## Skip every s pixels

Ques: Given p padding, $\mathrm{n} \times \mathrm{n}$ image, $\mathrm{f} \times \mathrm{f}$ filter, s stride, what is output length?

## Building Block: Strides (subsampling)

Skip every s pixels
Ques: Given p padding, $\mathrm{n} \times \mathrm{n}$ image, $\mathrm{f} \times \mathrm{f}$ filter, s stride, what is output length?

$$
\lfloor(n+2 p-f) / s\rfloor+1 \times L(n+2 p-f) / s\rfloor+1
$$

## Building Block: Pooling (subsampling)

| 3 | 3 | 2 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 3 | 1 |
| 3 | 1 | 2 | 2 | 3 |
| 2 | 0 | 0 | 2 | 2 |
| 2 | 0 | 0 | 0 | 1 |

Max pooling

| 3.0 | 3.0 | 3.0 |
| :--- | :--- | :--- |
| 3.0 | 3.0 | 3.0 |
| 3.0 | 2.0 | 3.0 |

Similar to filter and convolution operation, but, gives the max value in the $\mathrm{f} \times \mathrm{f}$ as the output

## Building Block: Pooling (subsampling)

| 3 | 3 | 2 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 3 | 1 |
| 3 | 1 | 2 | 2 | 3 |
| 2 | 0 | 0 | 2 | 2 |
| 2 | 0 | 0 | 0 | 1 |

Max pooling

| 3.0 | 3.0 | 3.0 |
| :--- | :--- | :--- |
| 3.0 | 3.0 | 3.0 |
| 3.0 | 2.0 | 3.0 |

Similar to filter and convolution operation, but, gives the max value in the $\mathrm{f} \times \mathrm{f}$ as the output

Works well in practice Reduces representation size

## Building Block: Pooling (subsampling)

| 3 | 3 | 2 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 3 | 1 |
| 3 | 1 | 2 | 2 | 3 |
| 2 | 0 | 0 | 2 | 2 |
| 2 | 0 | 0 | 0 | 1 |

Average pooling
Similar to filter and convolution operation, but, gives the average value in the fx f as the output

Works well in practice Reduces representation size

## Building Block: Multiple channels



Input: $\mathrm{n} \times \mathrm{n} \times \mathrm{c}$ image

## Building Block: Multiple channels



Input: $\mathrm{n} \times \mathrm{n} \times \mathrm{c}$ image

Filter for $r$ channel: fxf

## Building Block: Multiple channels



Input: n x n x c image

Filter for $r$ channel: fxf

Output for $r$ channel: $n-f+1 x$ $n-f+1$

## Building Block: Multiple channels



Input: n x n x c image

Filter for g channel: fxf

Output for $g$ channel: $n-f+1 x$ $n-f+1$

## Building Block: Multiple channels



Input: n x n x c image

Filter for b
channel: fxf

Output for b channel: $n-f+1 x$ $n-f+1$

## Building Block: Multiple channels



Input: $\mathrm{n} \times \mathrm{n} \times \mathrm{c}$ image


Output for 3 channel: $\mathrm{n}-\mathrm{f}+1 \mathrm{x}$ $n-f+1 \times 1$

## Building Block: Non-linearity



## $g(\square+b)$

Input: $\mathrm{n} \times \mathrm{n} \times \mathrm{c}$ image

Filter for 3
channel: $\mathrm{fx} \mathrm{f} \times 3$

Activation Output for 3 channel:

$$
n-f+1 \times n-f+1 \times 1
$$

## Exercise LeNet-5



## Exercise LeNet-5

Q1: What is input size?


## Exercise LeNet-5

Q1: What is input
size?
32X32X1
(grayscale)


## Exercise LeNet-5

Q2: What is filter size for first layer (assume no padding)


## Exercise LeNet-5

Q2: What is filter size for first layer (assume no padding, 1 stride)
$5 \times 5: 32 \rightarrow 32-5+1=28$


## Exercise LeNet-5

Q3: What is number of
filters used in first layer?


## Exercise LeNet-5

Q3: What is number of
filters used in first layer?
6


## Exercise LeNet-5

Q4: What is size of pool filter?


## Exercise LeNet-5

Q4: What is size of pool filter?
$\mathrm{f}=2, \mathrm{~s}=2$ (stride 2 )


## Exercise LeNet-5

Q5: What is size of filter for this layer convolution?


## Exercise LeNet-5

Q5: What is size and number of filter for this layer convolution?

16 filter $5 \times 5$ size with stride 1


## Exercise LeNet-5

Q6: What is size of this
pool layer?


## Exercise LeNet-5

Q6: What is size of this
pool layer?
$f=2, s=2$


## Exercise LeNet-5

Q7: This layer is connected to an MLP like layer, how?


## Exercise LeNet-5

> Q7: This layer is connected to an MLP like layer, how?

We flatten 16X5X5 to create a 400X1 matrix


## Exercise LeNet-5



## Exercise LeNet-5

What is the total number of parameters?


## Exercise LeNet-5

What is the total number of parameters?

- CONV1: 6 filters of size $5 \mathrm{X} 5 \mathrm{X} 1($ channel $)=(6 * 5 * 5)+6$ biases $=156$
- POOL1: No params
- CONV2: 16 filters of size $5 \times 5 \times 6$ (six channels $)=\left(16^{*} 5^{*} 5^{*} 6\right)+16$ biases $=2416$
- FC1: Weight matrix of size $120 \times 400+120$ biases $=48120$
- FC2: Weight matrix of size $84 \times 120+84$ biases $=10164$
- FC3: Weight matrix of size $10 \times 84+10$ biases $=850$
- Total $=61,706$



## Notebook: LeNet-5, AlexNet, VGG-16

- Notebook


## Training CNNs for own applications

- Train fully from scratch
- Transfer learning -- store activations


## Visualising CNNs

- t-SNE or PCA on last hidden layer ... MNIST
- Same exercise on Imagenet? ..

